

# Formula Key

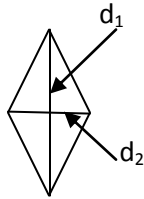
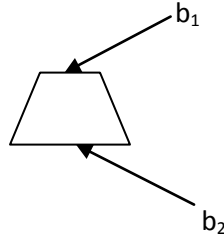
base      b or ( $b_1 / b_2$  for a *trapezoid*)

height    h

Area      A

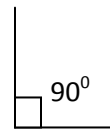
Perimeter P

diagonal    d ( $d_1 / d_2$  for a *kite*)



Perpendicular

two lines form a  $90^\circ$  angle.



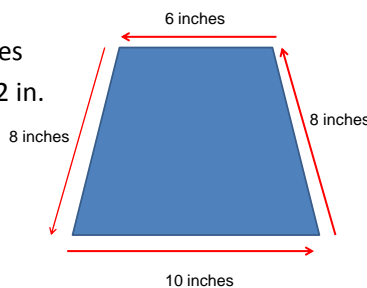
Perimeter

$P = \text{total of all sides (side + side + side + side...)}$

## Perimeter

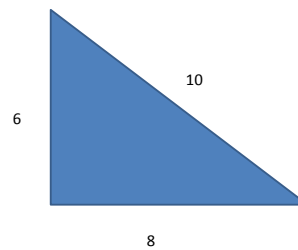
To find the perimeter of any shape **add** all the **side lengths** together.

$8+10+8+6=32$  inches  
The perimeter is 32 in.



## Pythagorean Theorem

$$A^2 + B^2 = C^2$$



$$6^2 + 8^2 = 10^2$$

$$36 + 84 = 100$$

$$C^2 = 100$$

$$C = \sqrt{100}$$

$$C = 10$$

Area of a triangle       $A = \frac{1}{2} \times b \times h$  or  $\frac{1}{2}bh$  or  $\frac{bh}{2}$

Area of a rectangle       $A = b \times h$  or  $bh$

Area of a parallelogram       $A = b \times h$  or  $bh$  (Same as a rectangle)

Area of a trapezoid       $A = \frac{1}{2} \times (b_1 + b_2) \times h$  or  $\frac{1}{2}(b_1 + b_2)h$  or  $\frac{(b_1 + b_2)h}{2}$

Area of a kite       $A = \frac{1}{2} \times d_1 \times d_2$  or  $\frac{1}{2}d_1d_2$  or  $\frac{d_1d_2}{2}$

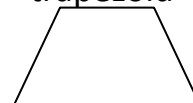
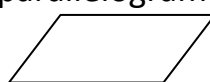
triangle

rectangle

parallelogram

trapezoid

kite



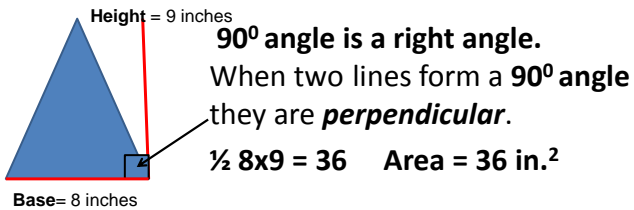
## Area of a Triangle

Formula:  $\frac{1}{2} \times \text{base} \times \text{height}$  or  $\frac{1}{2} b \times h$  or  $\frac{1}{2} bh$

The **base** is measured by length

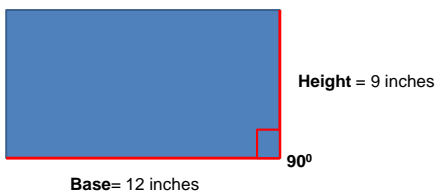
The **height** is measured by length

The **height** and the **base** must form a **90° angle**.



## Area of a Rectangle

Formula:  $\text{base} \times \text{height}$  or  $b \times h$  or **bh**



The **base** and the **height** must be **perpendicular**.

**Perpendicular** = two lines form a right angle. (90°)

**Base x height = Area**  $12 \times 9 = 108$  Area = 108 in.<sup>2</sup>

## Area of Kites

Formula:  $\text{Area} = \frac{1}{2} \text{diagonal}_1 \times \text{diagonal}_2$

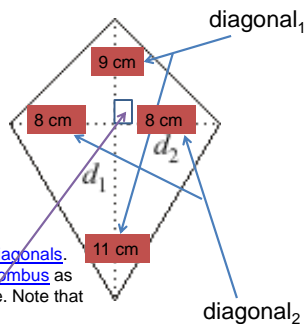
$$d_1 = (9\text{cm} + 11\text{cm})$$

$$d_2 = (8\text{cm} + 8\text{cm})$$

$$A = \frac{1}{2} \times d_1 \times d_2$$

$$A = \frac{1}{2} \times 20 \times 16$$

$$A = 160 \text{ cm}^2$$

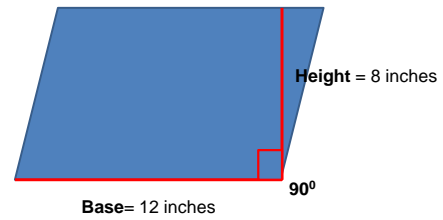


The area of a **kite** is half the **product** of the **diagonals**.  
 Note: This **formula** works for the **area of a rhombus** as well, since a **rhombus** is a special kind of kite. Note that the diagonals of a kite are **perpendicular**.

## Area of a Parallelogram

Formula:  $\text{base} \times \text{height}$  or  $b \times h$  or **bh**

$$12 \times 8 = 96 \quad \text{Area} = \underline{96 \text{ in.}^2}$$



*\*Use the same formula as a rectangle*

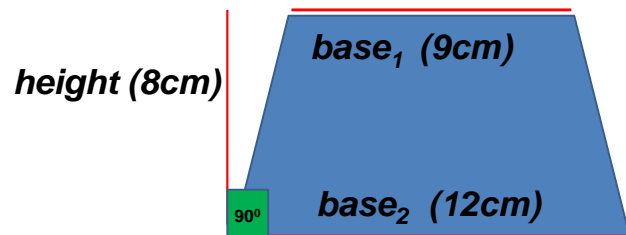
## Area of a Trapezoid

Formula:  $\text{Area} = \frac{1}{2} (\text{base}_1 + \text{base}_2) \times \text{height}$

$$A = \frac{1}{2} (b_1 + b_2) \times h$$

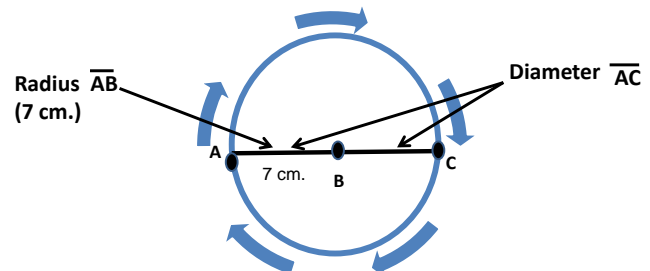
$$A = \frac{1}{2} (9 + 12) \times 8$$

$$A = 84 \text{ cm}^2$$



## Area of a Circle Using Radius

**Definition:** the inside of circle



**Formulas:**  $\text{Area} = \pi \times \text{radius}^2$  or  $A = \pi r^2$

$$\text{Area} = \pi \times (7 \text{ cm.})^2 \text{ or } A = \pi(7^2)$$

$$\text{Area} = \pi \times 49 \quad A = 49\pi \quad A = 154 \text{ cm.}$$

## Formula Key for Circles

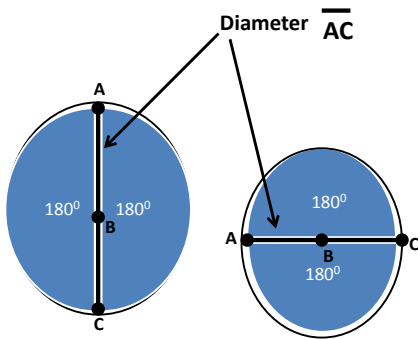
Diameter is 2 x radius. ( $2r$ )

It is a **line segment** that divides a circle in half.

Each half is called a **semi-circle**.

The diameter crosses through the **center point**.

### Diameter

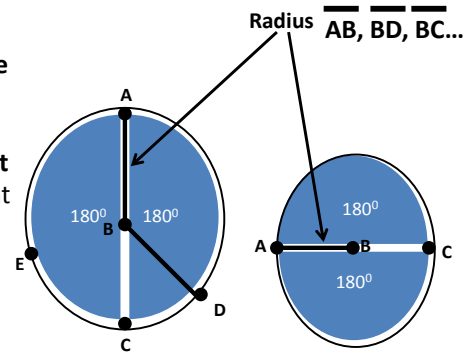


The radius is  $\frac{1}{2}$  the diameter. ( $\frac{1}{2}d$ )

It is a **line segment** with **one end point** on the **center** and **one end point** on the **edge** of the circle.

A circle can have many radii.

### Radius



## *Equations to find Diameter & Radius*

**Radius** = 7cm.

$2 \times \text{radius} = \text{diameter}$

$2 \times 7 = d$

$d = 14$

**Diameter** = 14 cm

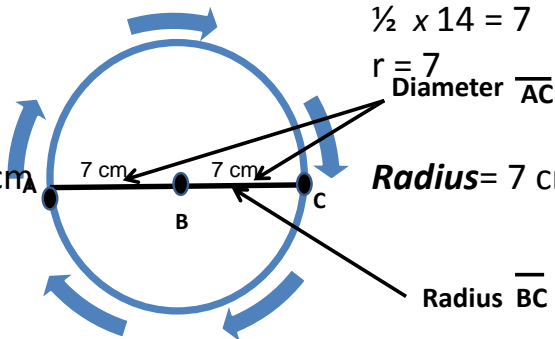
$\frac{1}{2} \times \text{diameter} = \text{radius}$

$\frac{1}{2} \times 14 = 7$

$r = 7$

**Diameter** = 14 cm

**Radius** = 7 cm

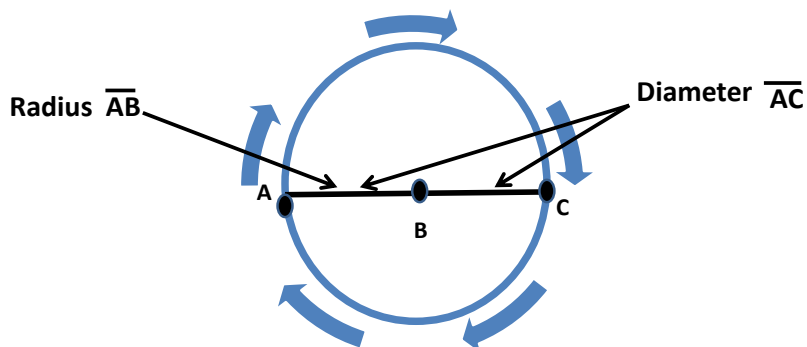


**Formulas:** **diameter** =  $2 \times \text{radius}$  or  $2r$

**radius** =  $\frac{1}{2} \times \text{diameter}$  or  $\frac{1}{2}d$

# Circumference

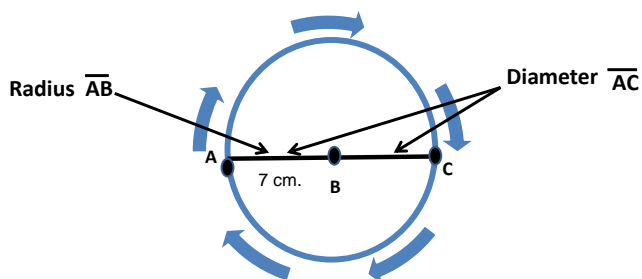
**Definition:** The distance around the whole circle



**Formulas:** Circumference =  $\pi \times \text{diameter}$  or  $C = \pi d$   
 Circumference =  $2 \times \pi \times \text{radius}$  or  $C = 2\pi r$

## Circumference using diameter:

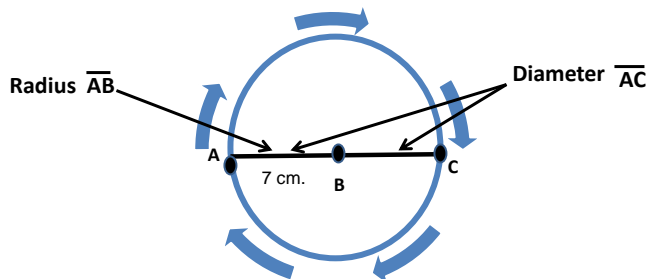
**Diameter** = 14 cm.  $C = \pi d$  or  $C = 14\pi$   $C = 44$  cm.



**Formulas:** Circumference =  $\pi \times \text{diameter}$  or  $C = \pi d$   
Circumference =  $2 \times \pi \times \text{radius}$  or  $C = 2\pi r$

## Circumference using radius:

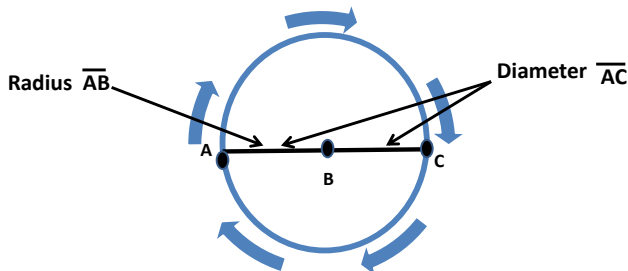
**Radius** = 7cm.  $C = 2 \times \pi \times r$ ,  $C = 2\pi r$ ,  $C = 14\pi$ ,  $C = 44$  cm.



**Formulas:** Circumference =  $\pi \times \text{diameter}$  or  $C = \pi d$   
Circumference =  $2 \times \pi \times \text{radius}$  or  $C = 2\pi r$

## Area of a Circle

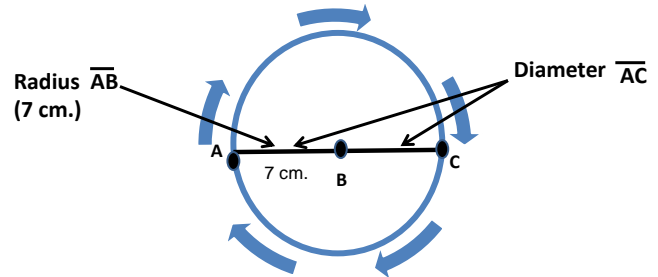
**Definition:** the inside of circle



**Formulas:** Area =  $\pi \times \text{radius}^2$  or  $A = \pi r^2$   
 Area =  $\pi \times (\frac{1}{2} \text{diameter})^2$  or  $A = \pi(\frac{1}{2}d)^2$

## Area of a Circle Using Radius

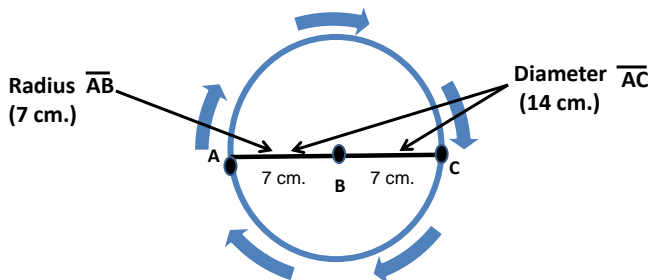
**Definition:** the inside of circle



**Formulas:** Area =  $\pi \times \text{radius}^2$  or  $A = \pi r^2$   
 Area =  $\pi \times (7 \text{ cm.})^2$  or  $A = \pi(7^2)$   
 Area =  $\pi \times 49$   $A = 49 \pi$   $A = 154 \text{ cm.}$

## Area of a Circle Using Diameter

**Definition:** the inside of circle



**Formulas:** Area =  $\pi \times (\frac{1}{2} \text{diameter})^2$  or  $A = \pi(\frac{1}{2}d)^2$   
 Area =  $\pi \times (\frac{1}{2}14 \text{ cm.})^2$  or  $A = \pi(7^2)$   
 Area =  $\pi \times 49$   $A = 49 \pi$   $A = 154 \text{ cm.}$

## Major and Minor Arcs

The Symbol is

The minor arc is less than  $180^\circ$

The major arc is more than  $180^\circ$

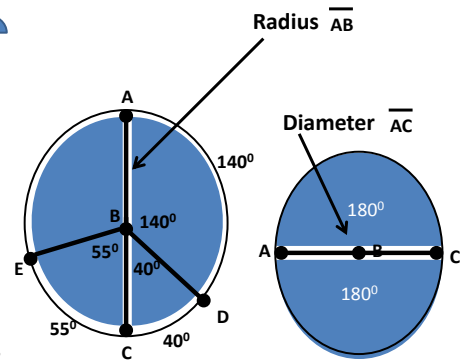
AD is a minor arc

AD =  $140^\circ$

ADE is a major arc.

ADE =  $140 + 40 + 55$

ADE =  $235^\circ$



What does AE equal?  $360^\circ - 235^\circ = 145^\circ$

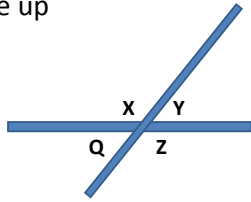
\*Note- The major arc will have three vertices to show direction.

# Interior Angles of shapes & Lines

## Straight Lines

The angles that make up a line **always** equal 180 degrees.

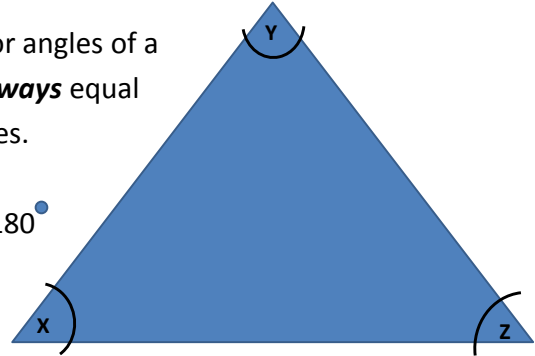
$$\begin{aligned} \angle X + \angle Y &= 180 \\ \angle Y + \angle Z &= 180 \\ \angle Z + \angle Q &= 180 \\ \angle Q + \angle X &= 180 \end{aligned}$$



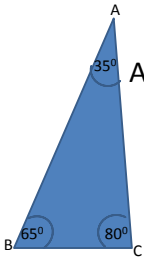
## Triangles

The interior angles of a triangle **always** equal **180** degrees.

$$X + Y + Z = 180$$



## Angles



The symbol for an angle is  $\angle$   
 Angles are measured in **degrees**.  
 The symbol for degrees is  $^{\circ}$

Examples:

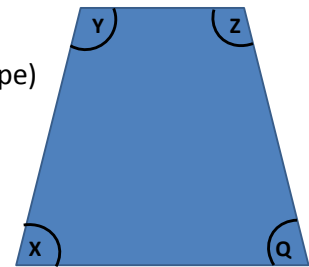
$$\begin{aligned} (\text{Angle A}) \angle A &= 35^{\circ} \\ (\text{Angle B}) \angle B &= 65^{\circ} \\ (\text{Angle C}) \angle C &= 80^{\circ} \end{aligned}$$

The sum (total) of interior (inside) angles of a **triangle** is always **180**  
 $35 + 65 + 80 = 180$

## Quadrilateral

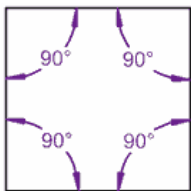
The interior angles of a Quadrilateral (4 sided shape) **always** equal **360** degrees.

$$X + Y + Z + Q = 360$$



## Quadrilaterals (Squares, etc)

(A Quadrilateral has 4 straight sides)

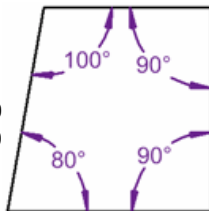


$$90^{\circ} + 90^{\circ} + 90^{\circ} + 90^{\circ} = 360^{\circ}$$

A Square adds up to 360°

**Formula:**

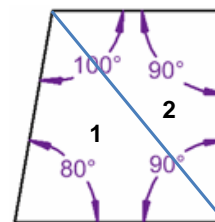
$$\begin{aligned} 180(n-2) &= 360 \\ 180(4-2) &= 360 \\ 180(2) &= 360 \end{aligned}$$



$$80^{\circ} + 100^{\circ} + 90^{\circ} + 90^{\circ} = 360^{\circ}$$

Let's tilt a line by 10° ... still adds up to 360°!

Divide the shape into triangles :



A quadrilateral can be divided into two triangles. Each triangle has 3 angles that add up to 180°.  $2 \times 180^{\circ} = 360^{\circ}$ .